

数学与系统科学研究院

计算数学所学术报告

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报告题目:

**Certification via Symbolic-Numeric  
Computations**

邀请人: 优化与应用研究中心

报告时间: **2010 年 12 月 15 日 (周三)**

**下午 15: 00-16: 00**

报告地点: **科技综合楼三层 311**

**计算数学所报告厅**

## **Abstract:**

We present a hybrid symbolic-numeric algorithm for certifying a polynomial or a rational function with rational coefficients to be non-negative for all real values of the variables by computing a representation for it as a fraction of two polynomial sum-of-squares (SOS) with rational coefficients. We can either perform high precision Newton iterations on the numerical SOS computed by SDP solvers in Matlab or use the high precision SDP solver in Maple to get the SOS with necessary precision, then we can convert the numerical SOS into an exact rational SOS by orthogonal projection or rational coefficient vector recovery. Sums-of-squares rational lower bound certificates for the radius of positive semidefiniteness of a multivariate polynomial also offer an alternative SOS proof for those positive definite polynomials that are not SOS but have a positive distance to the nearest polynomial with a real root. Moreover, we show that a random linear transformation of the variables allows with probability one for certifying the positive semidefiniteness of a multivariate polynomial by representing it as an SOS over the variety defined by partial derivatives of the polynomial with respect to each variable except one.

Joint work with Feng Guo, Sharon E. Hutton, Erich L. Kaltofen, Bin Li, Mohab Safey El Din and Zhengfeng Yang.

欢迎大家参加!