

数学与系统科学研究院

计算数学所学术报告

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报告题目:

**A new look at nonnegativity and
polynomial optimization**

邀请人: 优化与应用研究中心

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下午 16: 30-17: 30

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计算数学所报告厅

Abstract:

Obtaining tractable characterizations of functions which are nonnegative on a set $K \subset \mathbb{R}^n$ is a topic of primary importance. Indeed, such characterizations are highly desirable to help solve (or at least approximate) many important problems in various areas, and in particular, the global optimization problem:

$$P: \quad f^* = \min\{f(x) : x \in K\},$$

because solving P is equivalent to solving $f^* = \max\{\lambda : f - \lambda \geq 0 \text{ on } K\}$.

When f is a polynomial and K a basic semi-algebraic set, we have seen in the previous talk that Putinar's Positivstellensatz provides such tractable characterizations. Those characterizations depend on the representation of K through its defining polynomials.

In this talk we consider another way to look at continuous functions that are nonnegative on a (non necessarily compact basic semi-algebraic) set $K \subseteq \mathbb{R}^n$. This time, knowledge on K is through a finite Borel

measure μ with support $\text{supp } \mu = K$, and whose all moments

$y = (y_a), a \in N^n$, are available. This new characterization permits to

define convergent outer approximations of the convex cone $C_d(K)$ of polynomials of degree at most d , nonnegative on K , by a hierarchy of spectrahedra (convex sets defined by linear matrix inequalities) defined uniquely in terms of the coefficients of f . Important examples of cones $C_d(K)$ are the cone of nonnegative polynomials on \mathbb{R}^n and the cone of copositive matrices. Checking whether a fixed and known polynomial f is nonnegative on K reduces to solving a sequence of generalized eigenvalue problems for real symmetric matrices of increasing size.

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