

数学与系统科学研究院

计算数学所学术报告

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报告题目:

**Complexity of Unconstrained
L₂-L_p Minimization**

邀请人: 优化与应用研究中心

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上午 9: 00-10: 00

报告地点: **科技综合楼三层 311**

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Abstract:

We consider the unconstrained L_2 - L_p minimization: find a minimizer of $\|Ax-b\|_2^2 + \lambda \|x\|_p^p$ for given $A \in \mathbb{R}^{m \times n}$, $b \in \mathbb{R}^m$ and parameters $\lambda > 0$, $p \in [0,1)$. This problem has been studied extensively in variable selection and sparse least squares fitting for high dimensional data.

Theoretical results show that the minimizers of the L_2 - L_p problem have various attractive features due to the concavity and non-Lipschitzian property of the regularization function $\|\cdot\|_p^p$. In this paper, we show that the L_q - L_p minimization problem is strongly NP-hard for any $p \in [0,1)$ and $q \geq 1$, including its smoothed version. On the other hand, we show that, by choosing parameters (p, λ) carefully, a minimizer, global or local, will have certain desired sparsity. We believe that these results provide new theoretical insights to the studies and applications of the concave regularized optimization problems.

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