

数学与系统科学研究院

计算数学所学术报告

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报告题目:

**Spectral approximation of elliptic operators by the Hybrid High-Order method**

邀请人: 谢和虎 研究员

报告时间: **2019 年 4 月 15 日 (周一)**

**上午 10:00-11:00**

报告地点: **科技综合楼三层**

**311 报告厅**

## **Abstract:**

The talk starts with Babuška's challenging questions raised in his recent emails on FEM spectrum and then discusses the approximation of elliptic operators by a recently-developed non-conforming method. We study the approximation of the spectrum of a second-order elliptic differential operator by the Hybrid High-Order (HHO) method. The HHO method is formulated using cell and face unknowns which are polynomials of some degree  $k > 0$ . The key idea for the discrete eigenvalue problem is to introduce a discrete operator where the face unknowns have been eliminated. Using the abstract theory of spectral approximation of compact operators in Hilbert spaces, we prove that the eigenvalues converge as  $h^{2t}$  and the eigenfunctions as  $h^t$  in the  $H^1$ -seminorm, where  $h$  is the mesh-size,  $t \in [s, k+1]$  depends on the smoothness of the eigenfunctions, and  $s > 1/2$  results from the elliptic regularity theory. The convergence rates for smooth eigenfunctions are thus  $h^{2k+2}$  for the eigenvalues and  $h^{k+1}$  for the eigenfunctions. Our theoretical findings, which improve recent error estimates for Hybridizable Discontinuous Galerkin (HDG) methods, are verified on various numerical examples including smooth and non-smooth eigenfunctions. Moreover, we observe numerically in one dimension for smooth eigenfunctions that the eigenvalues superconverge as  $h^{2k+4}$  for a specific value of the stabilization parameter.

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**欢迎大家参加！**